

# The effect of random uncertainties on CO<sub>2</sub> emissions from lakes

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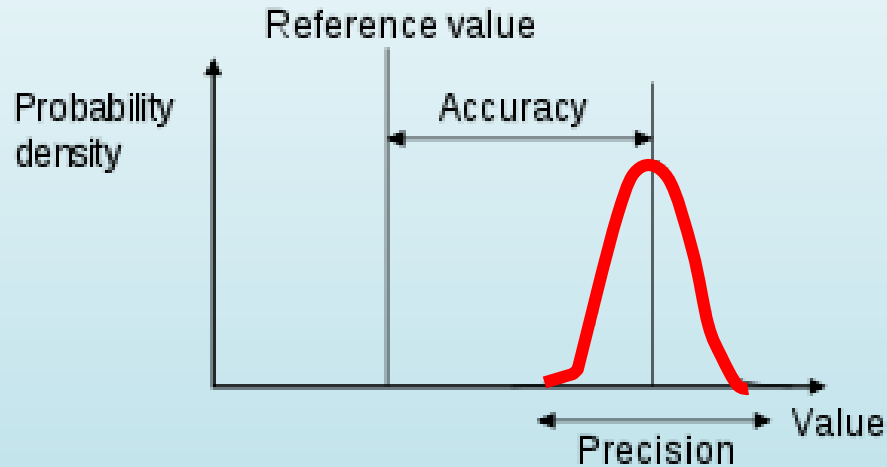
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JASM, May 21<sup>th</sup> 2014

# Accuracy vs. Precision



## **Systematic error** affects **accuracy**

- Instrumental errors
- Methodological limitations
- Personal errors

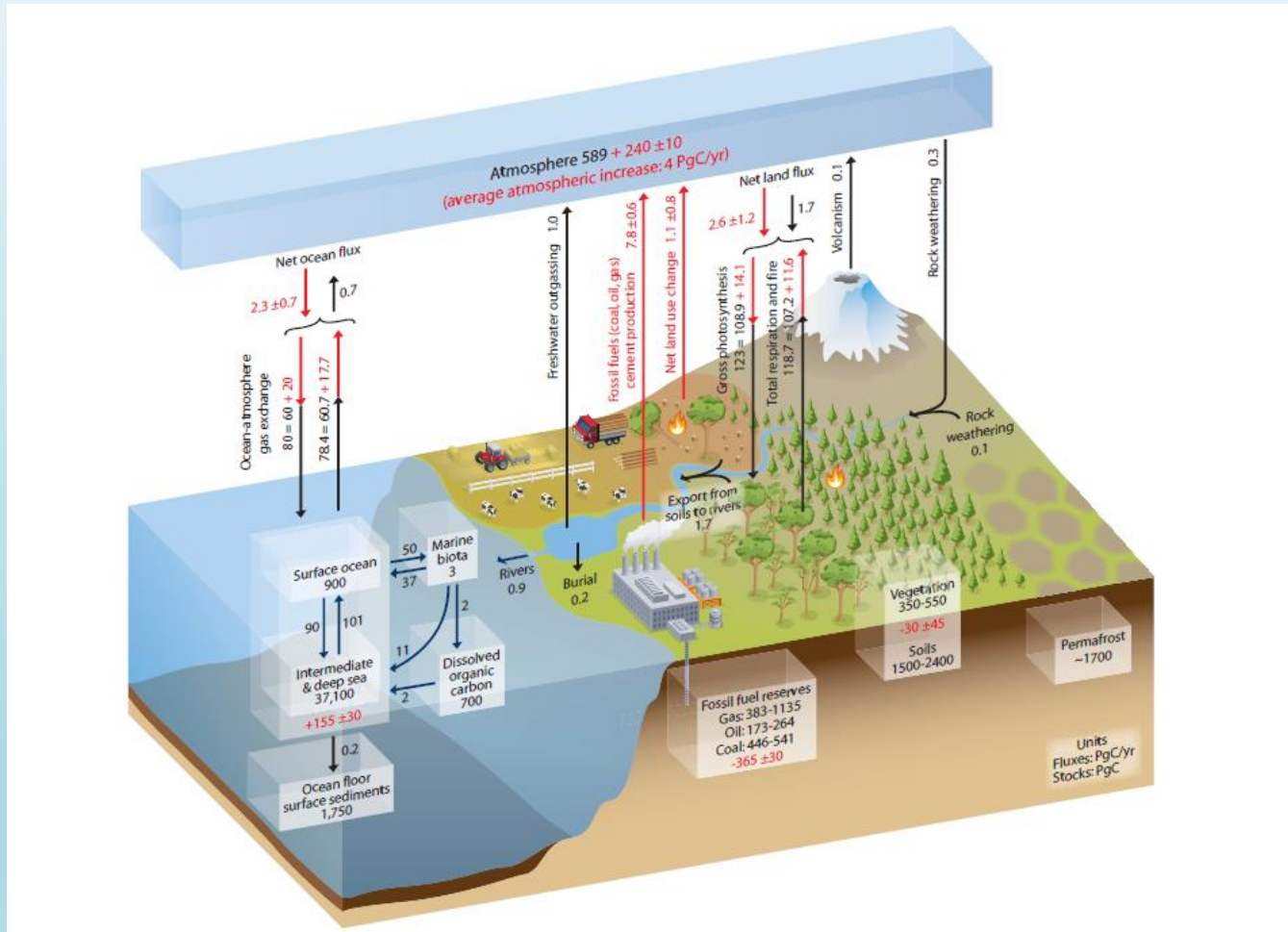
## **Random error** affects **precision**

- Caused by many hard to control variables

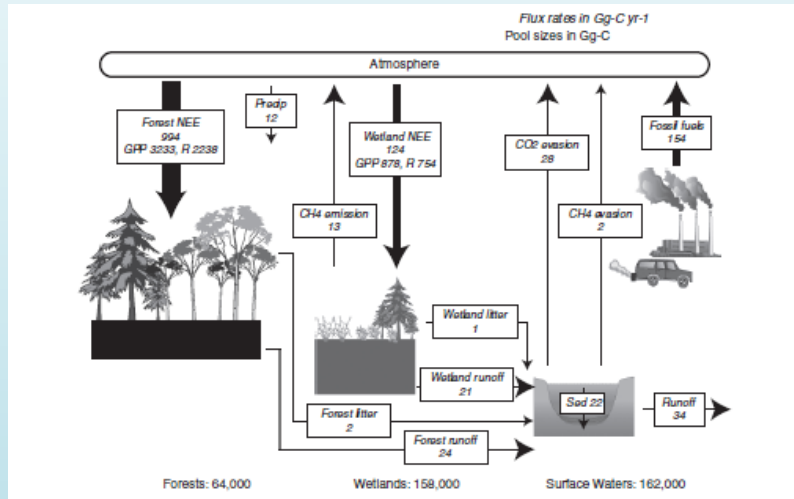
# Why random error matters?

- Unlike systematic errors we cannot remove random error effect (Bevington & Robinson 2003)
- Might be the largest source of uncertainty (Skoog et al., 2013)
- Needs to be taken into consideration during data analysis and interpretation (Hollinger and Richardson, 2005)
- Little attention paid but might have serious implications for comparisons across time and across site

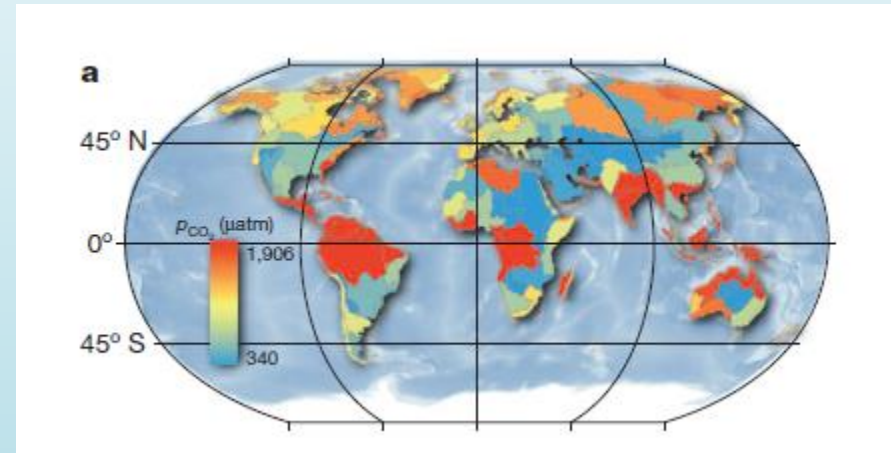
# Freshwater outgassing offsets 40% of net land flux



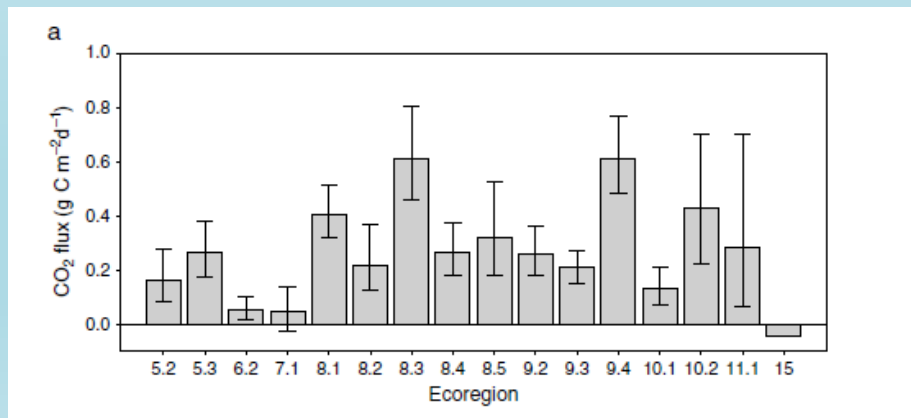
# Limited # of direct CO<sub>2</sub> measurements



Buffam et al., 2010



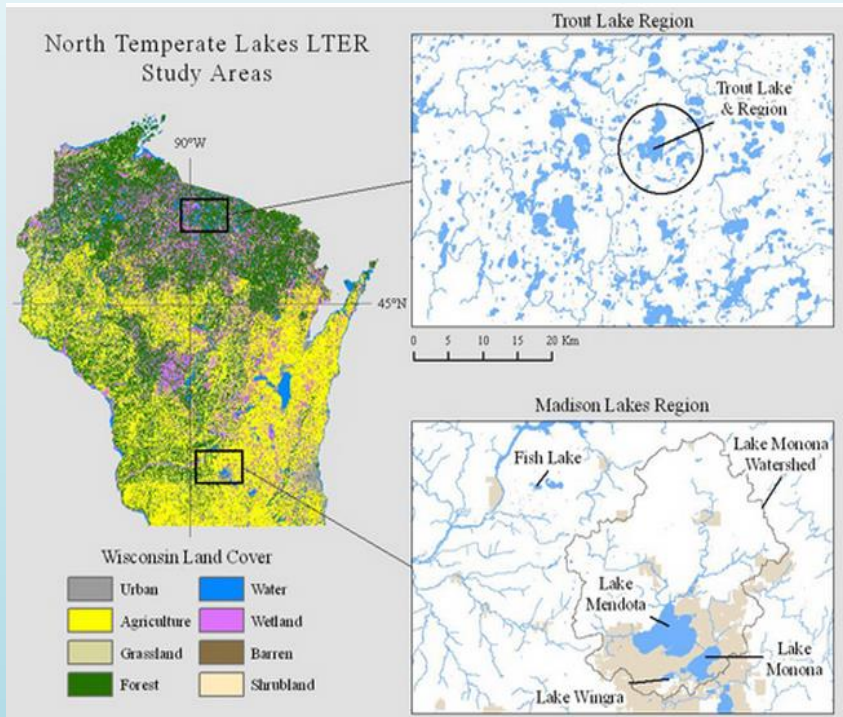
Raymond et al., 2013



McDonald et al., 2013

- CO<sub>2</sub> emissions often estimated from CO<sub>2</sub>-related parameters

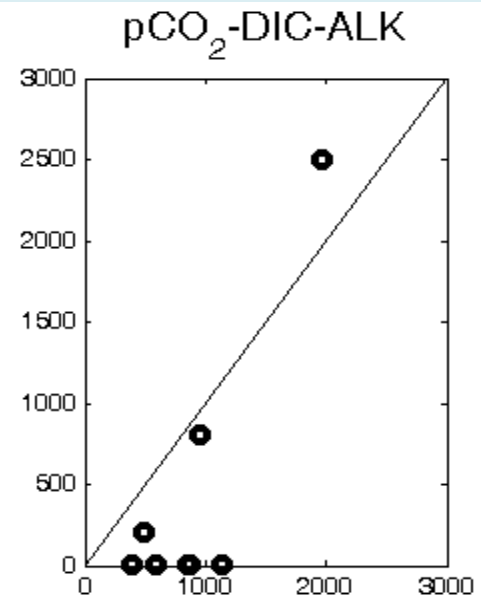
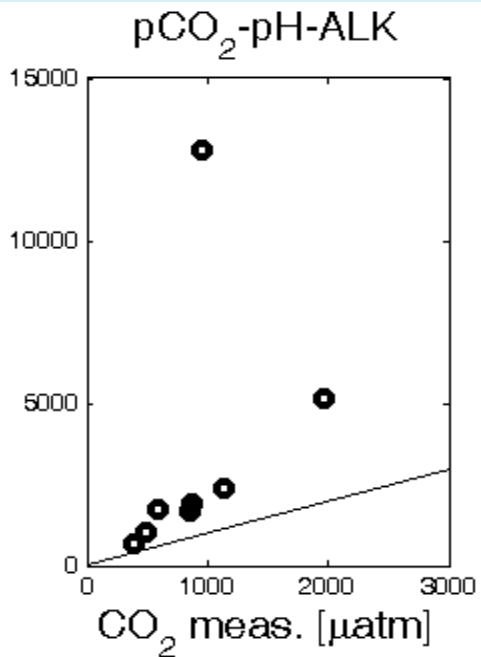
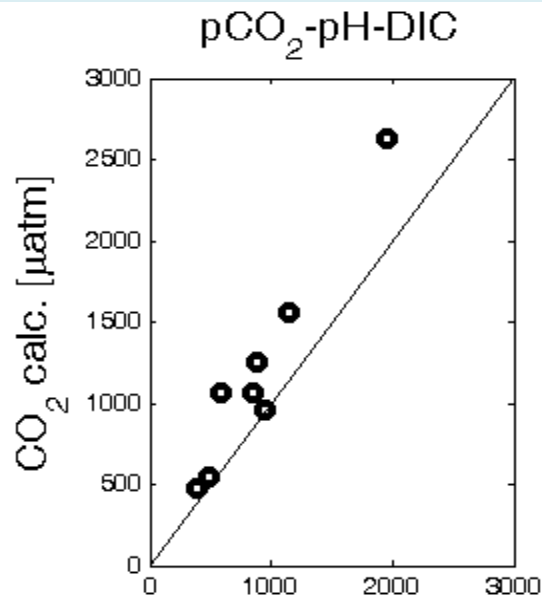
# North Temperate Lakes LTER site



- Limited direct CO<sub>2</sub> measurements
- CO<sub>2</sub>-related parameters data
  - **pH**
  - Alkalinity (**ALK**)
  - Dissolved Inorganic Carbon (**DIC**)
- Available:
  - Since 1986
  - Since 1996

**How reliably can we estimate CO<sub>2</sub> in lakes from CO<sub>2</sub>-related parameters?**

# Direct vs. Indirect CO<sub>2</sub> Mismatch



RMSE = **364** µatm

RMSE = **4410** µatm

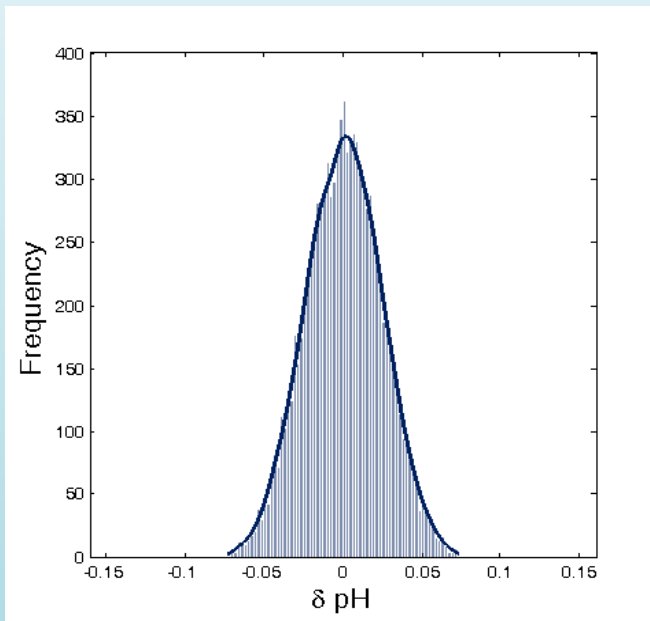
RMSE = **675** µatm

**How does observational error  
propagates into uncertainties of CO<sub>2</sub>  
estimates in lakes?**



# Random error calculated from paired samples

Low ALK

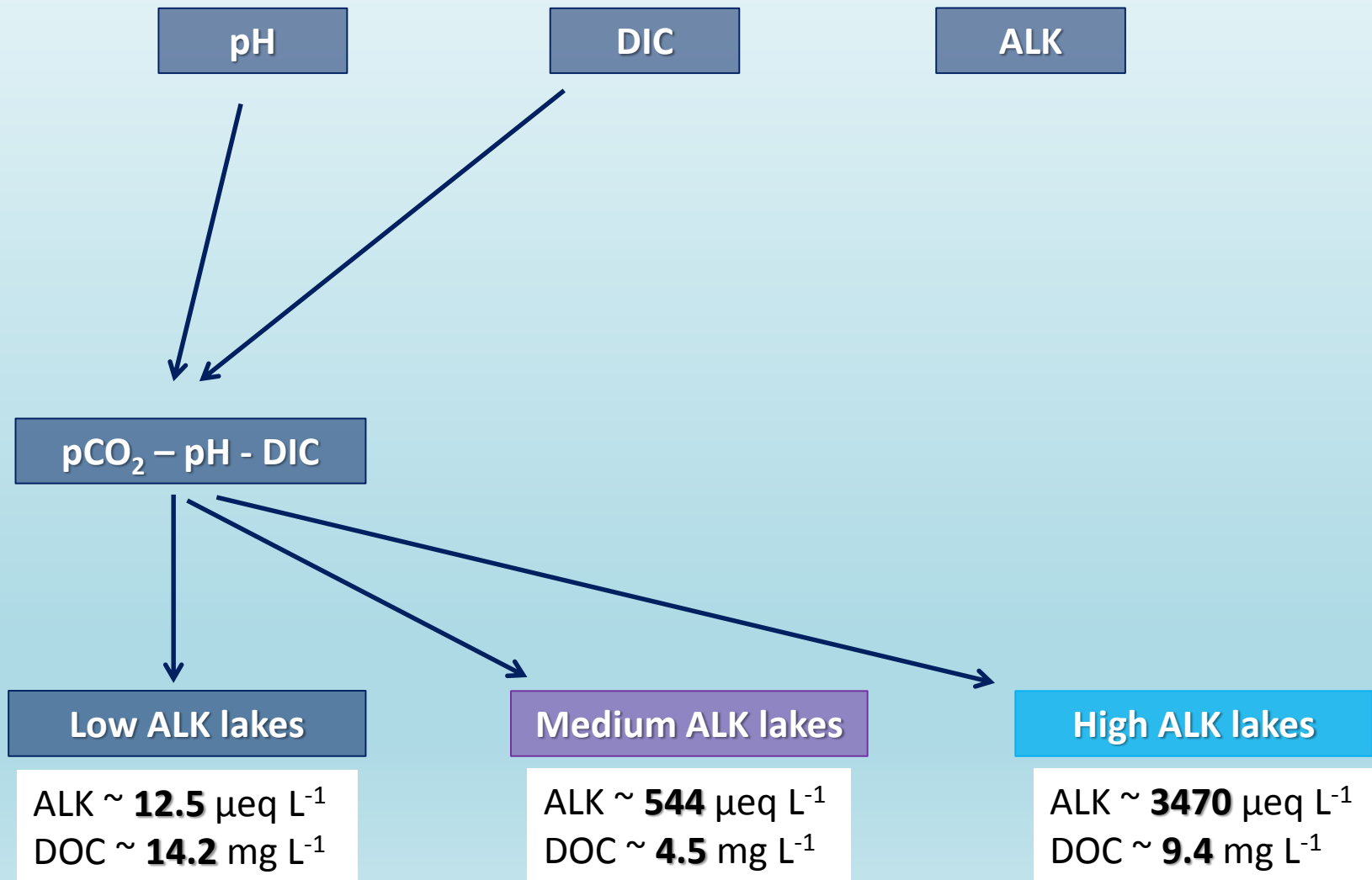


$$\mu = 0$$
$$\sigma(\delta) = 0.024$$

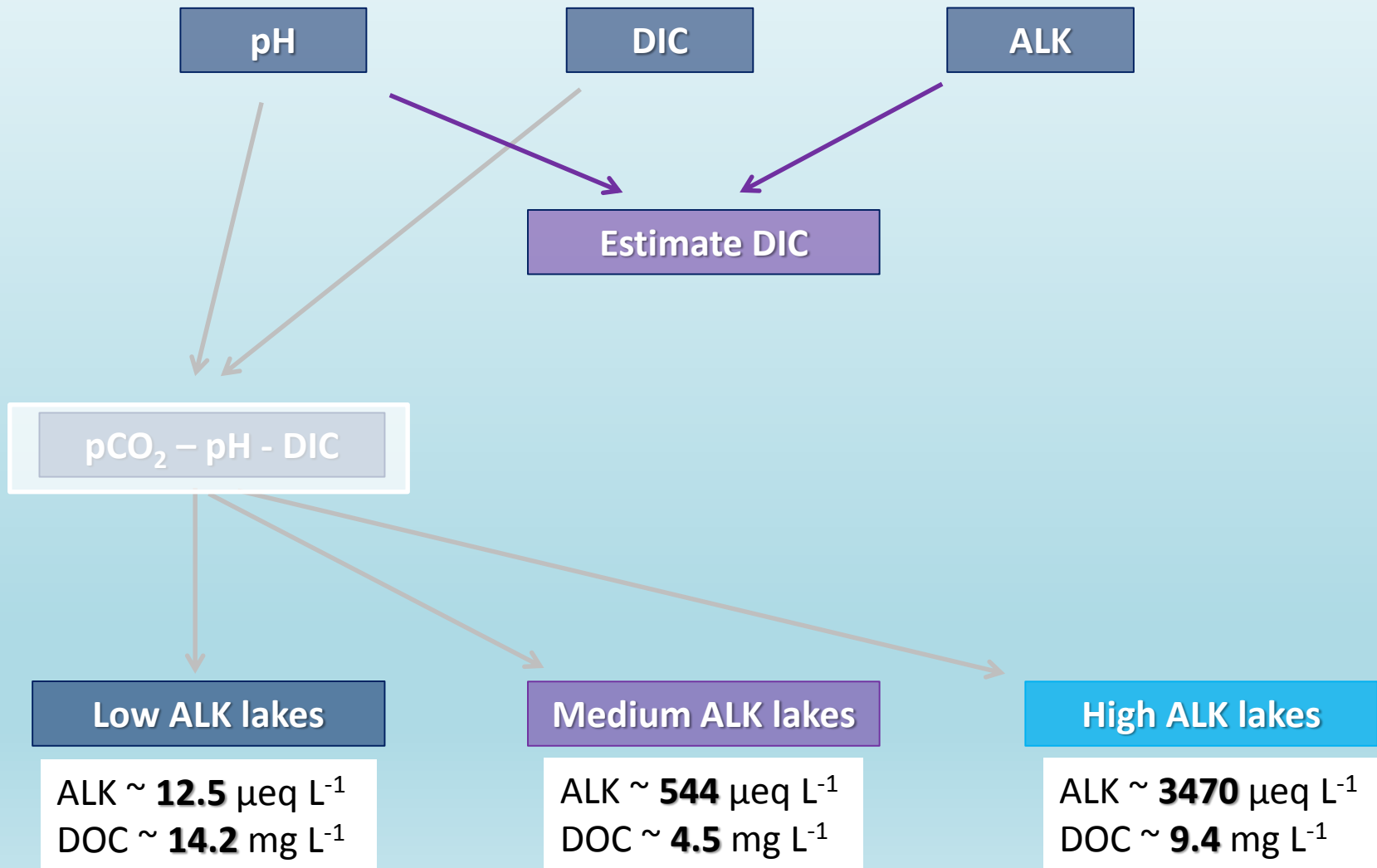
$$\sigma(\delta) = \frac{1}{\sqrt{2}} \sigma(X_1 - X_2)$$

- Probability distribution functions (PDFs) fitted to the error distribution
- The mean and standard deviation of the population estimated

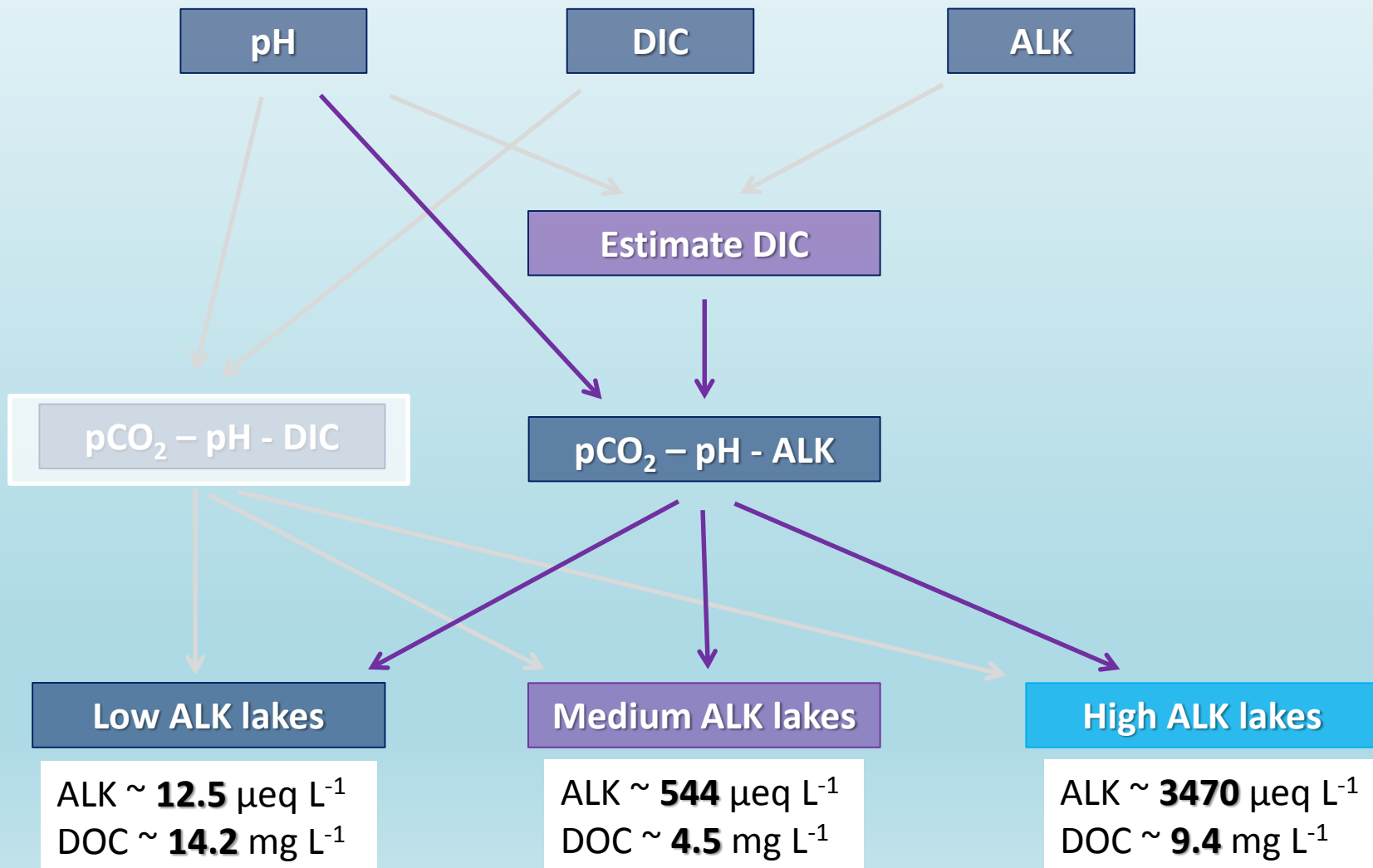
# Error Propagated Through Three Carbonate Equilibrium Constants Models



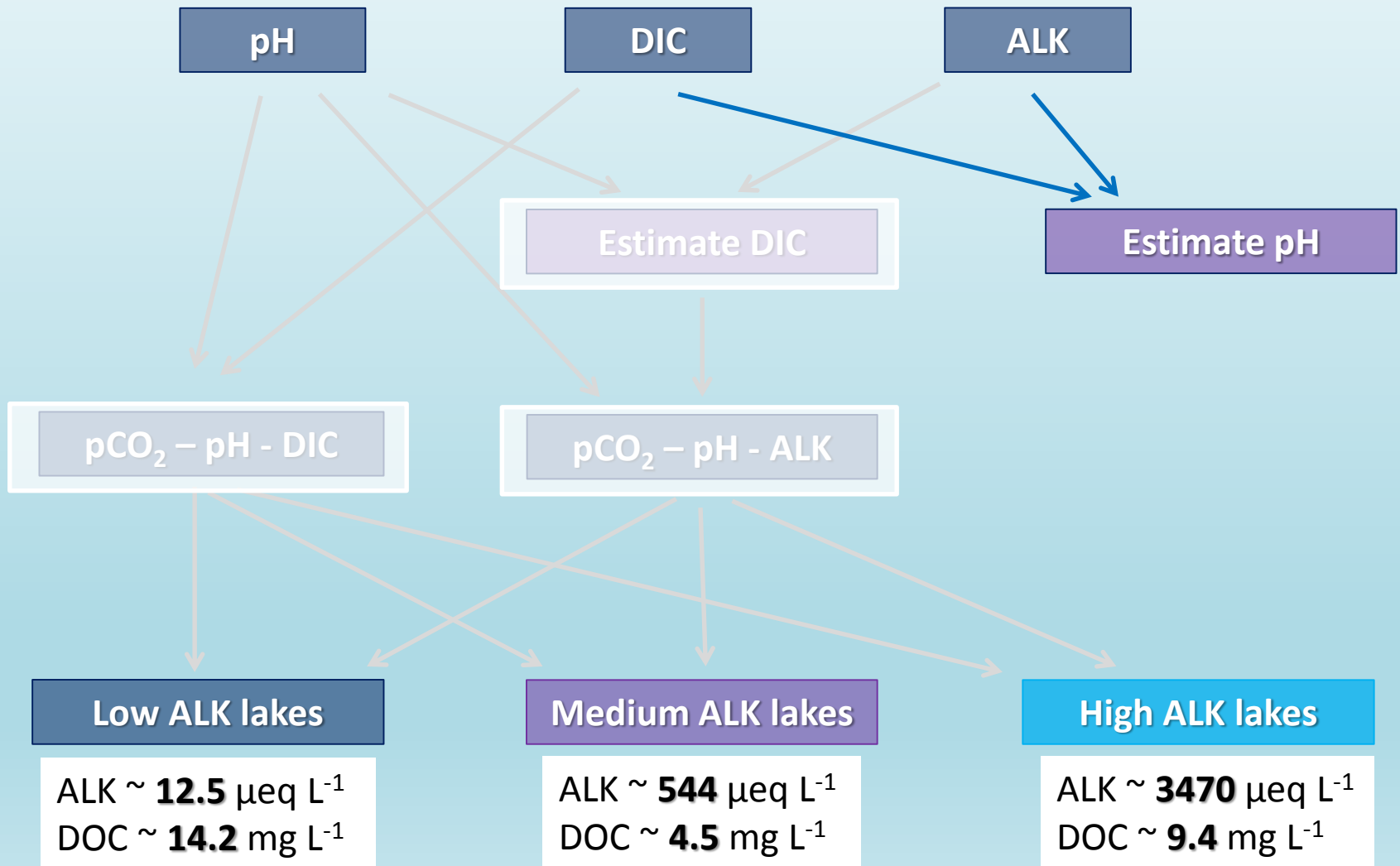
# Error Propagated Through Three Carbonate Equilibrium Constants Models



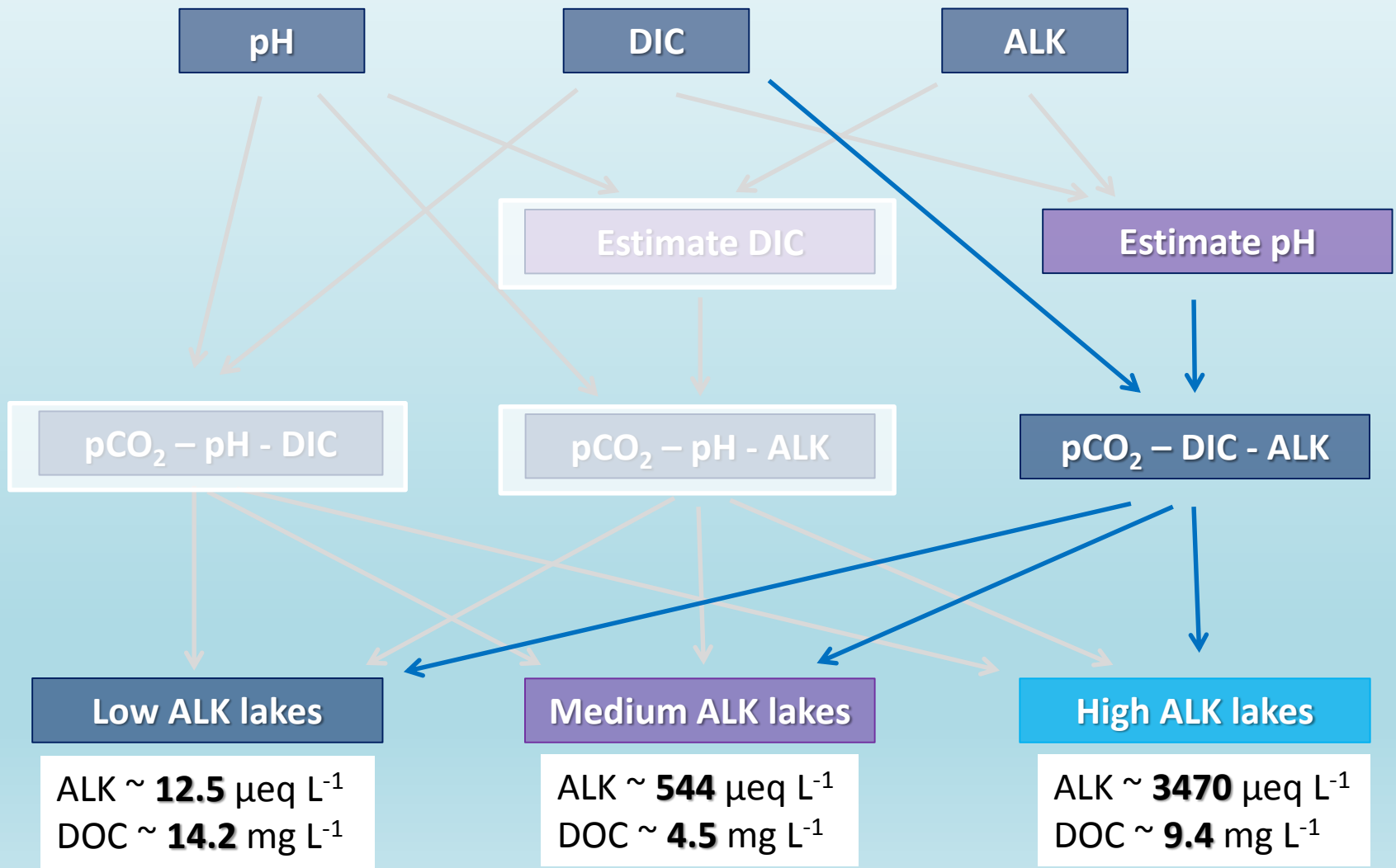
# Error Propagated Through Three Carbonate Equilibrium Constants Models



# Error Propagated Through Three Carbonate Equilibrium Constants Models



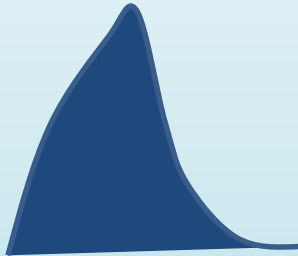
# Error Propagated Through Three Carbonate Equilibrium Constants Models



# Monte Carlo Technique

Parameters'  
Probability Density  
Functions

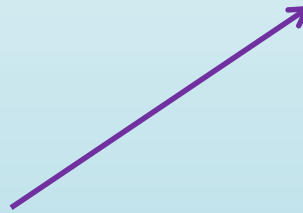
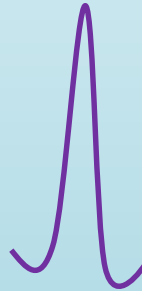
Random  
Error with  
 $\mu = 0$  &  $\sigma = X$



+



+

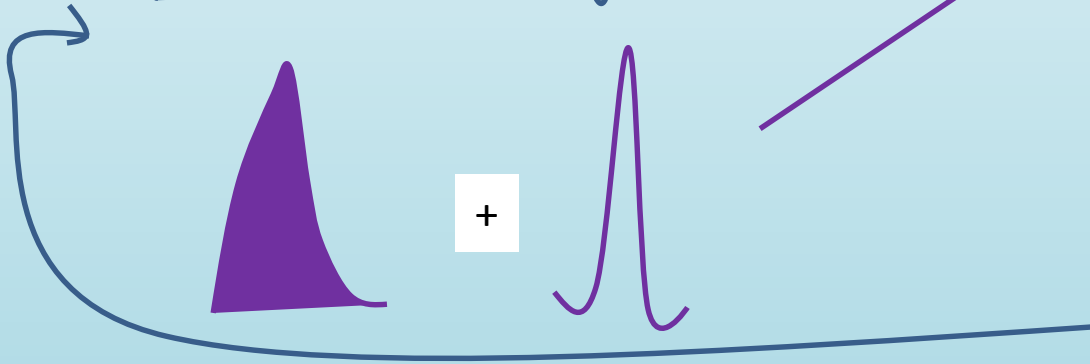


CO<sub>2</sub> Estimated using  
Three Carbonate  
Equilibrium Constants  
Models



Estimated Median,  
95% Credible  
Intervals at Each  
Iteration

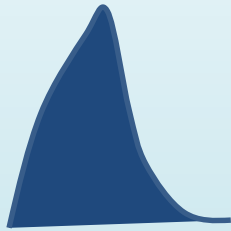
10,000  
iterations



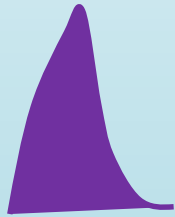
# Monte Carlo Technique

Parameters'  
Probability Density  
Functions

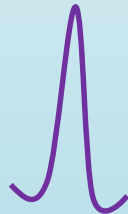
Random  
Error with  
 $\mu = 0$  &  $\sigma = X$



+



+



CO<sub>2</sub> Estimated using Three  
Carbonate Equilibrium  
Constants Models

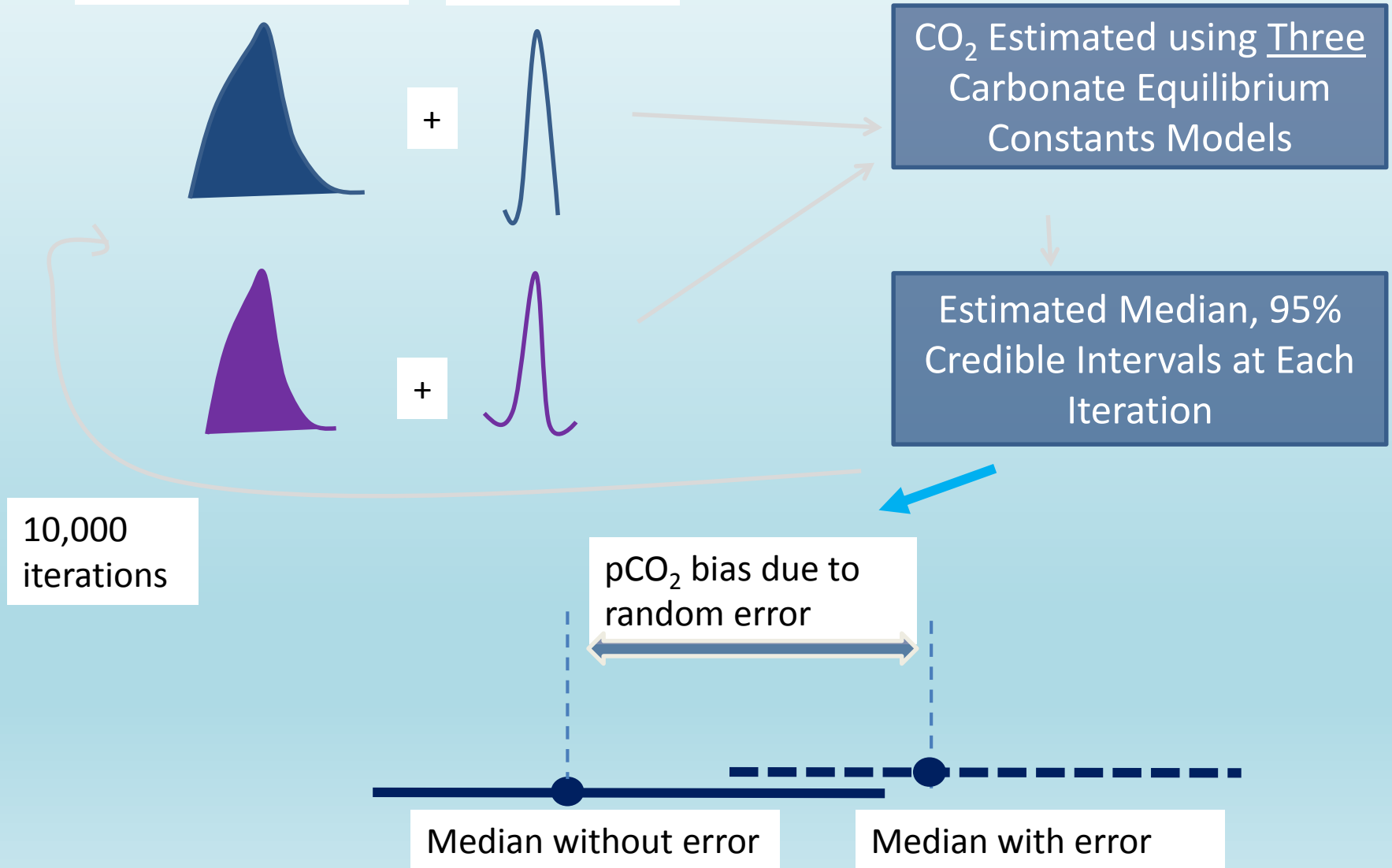
Estimated Median, 95%  
Credible Intervals at Each  
Iteration

10,000  
iterations

pCO<sub>2</sub> bias due to  
random error

Median without error

Median with error



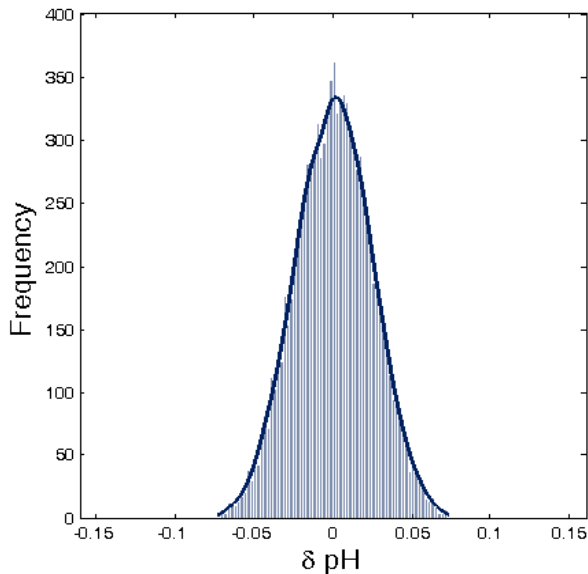


# **Estimates of errors in model parameters**

# Random parameter errors show normal or near-normal distribution

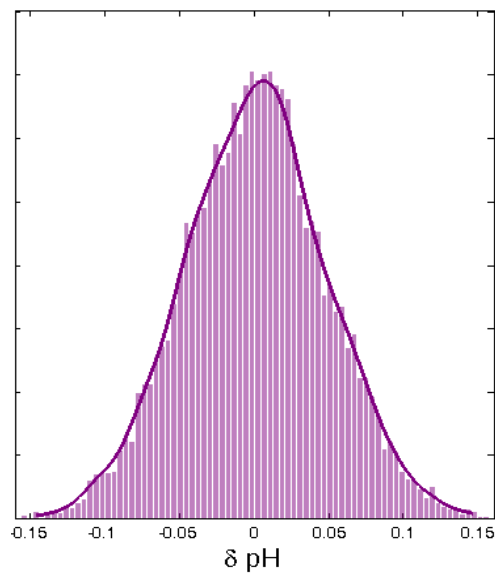
$$\sigma(\delta) = \frac{1}{\sqrt{2}} \sigma(X_1 - X_2)$$

Low ALK



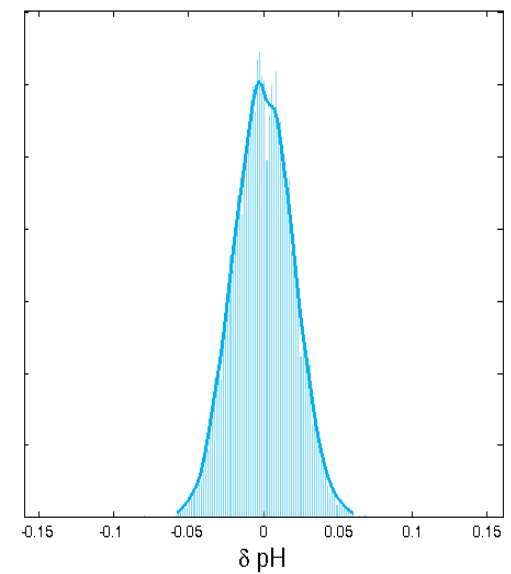
$$\mu = 0$$
$$\sigma = 0.024$$

Medium ALK



$$\mu = 0$$
$$\sigma = 0.048$$

High ALK



$$\mu = 0$$
$$\sigma = 0.019$$

# Largest random error in model parameters in medium ALK lakes

## High ALK

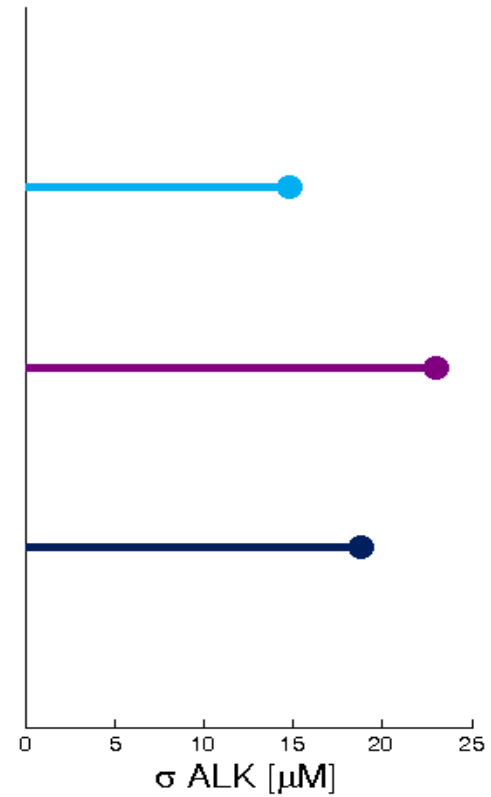
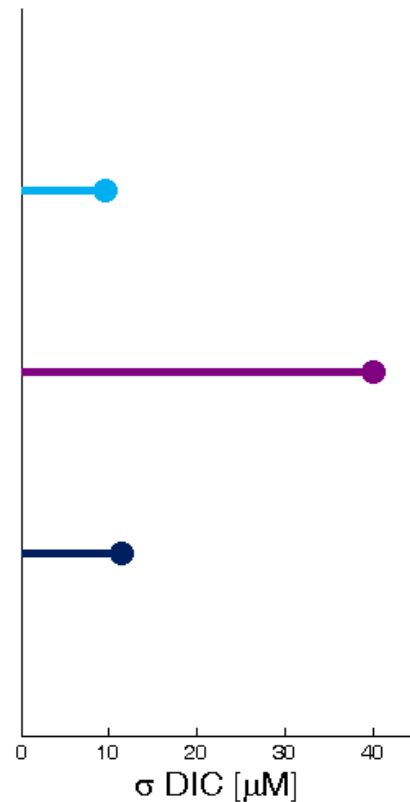
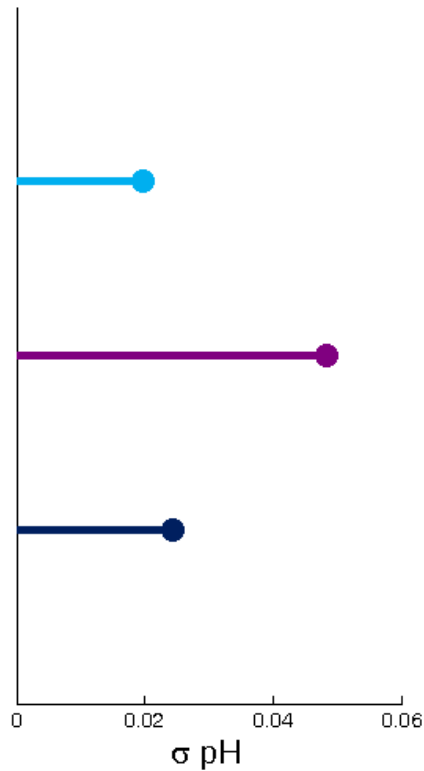
ALK ~ **3470**  $\mu\text{eq L}^{-1}$   
DOC ~ **9.4**  $\text{mg L}^{-1}$

## Med ALK

ALK ~ **544**  $\mu\text{eq L}^{-1}$   
DOC ~ **4.5**  $\text{mg L}^{-1}$

## Low ALK

ALK ~ **12.5**  $\mu\text{eq L}^{-1}$   
DOC ~ **14.2**  $\text{mg L}^{-1}$

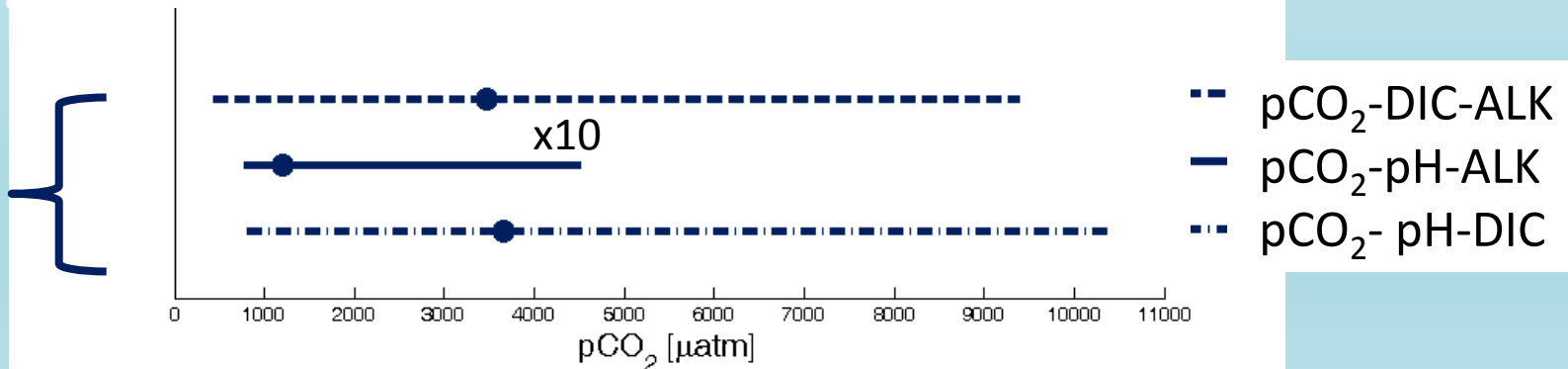


# **STEP 2: Random Error Propagation Through Carbonate Equilibrium Constant Models**

# pCO<sub>2</sub> – pH – ALK gives unrealistic pCO<sub>2</sub> estimates in low ALK lakes

## Low ALK

ALK ~ 12.5 μeq L<sup>-1</sup>  
DOC ~ 14.2 mg L<sup>-1</sup>



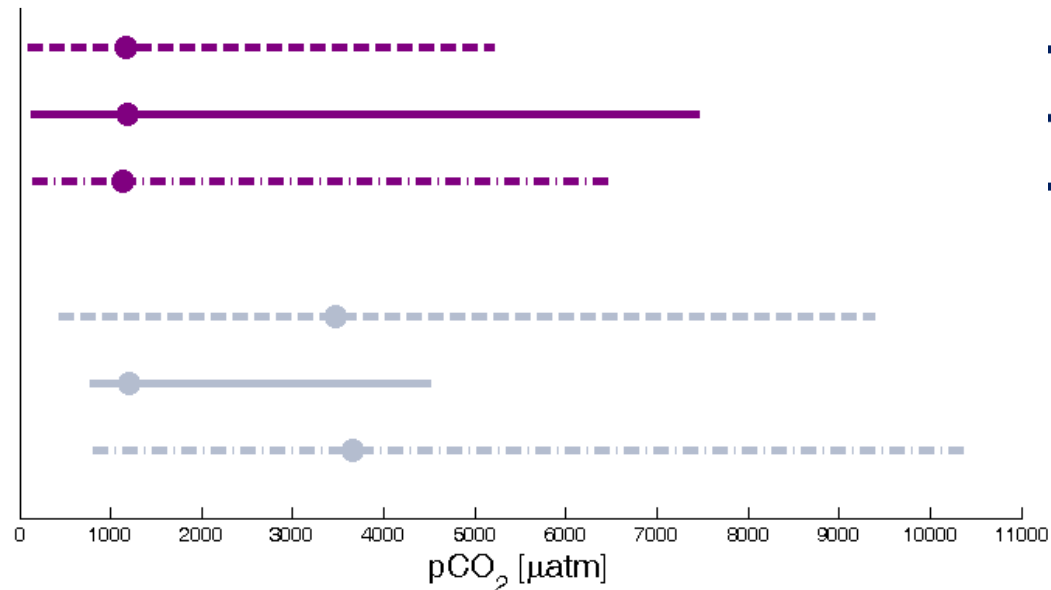
# Similar pCO<sub>2</sub> estimates in med-ALK regardless of model used

## Med ALK

ALK ~ 544  $\mu\text{eq L}^{-1}$   
DOC ~ 4.5  $\text{mg L}^{-1}$

## Low ALK

ALK ~ 12.5  $\mu\text{eq L}^{-1}$   
DOC ~ 14.2  $\text{mg L}^{-1}$



--- pCO<sub>2</sub>-DIC-ALK  
— pCO<sub>2</sub>-pH-ALK  
... pCO<sub>2</sub>-pH-DIC

# pH-based models give similar pCO<sub>2</sub> estimates in high ALK lakes

## High ALK

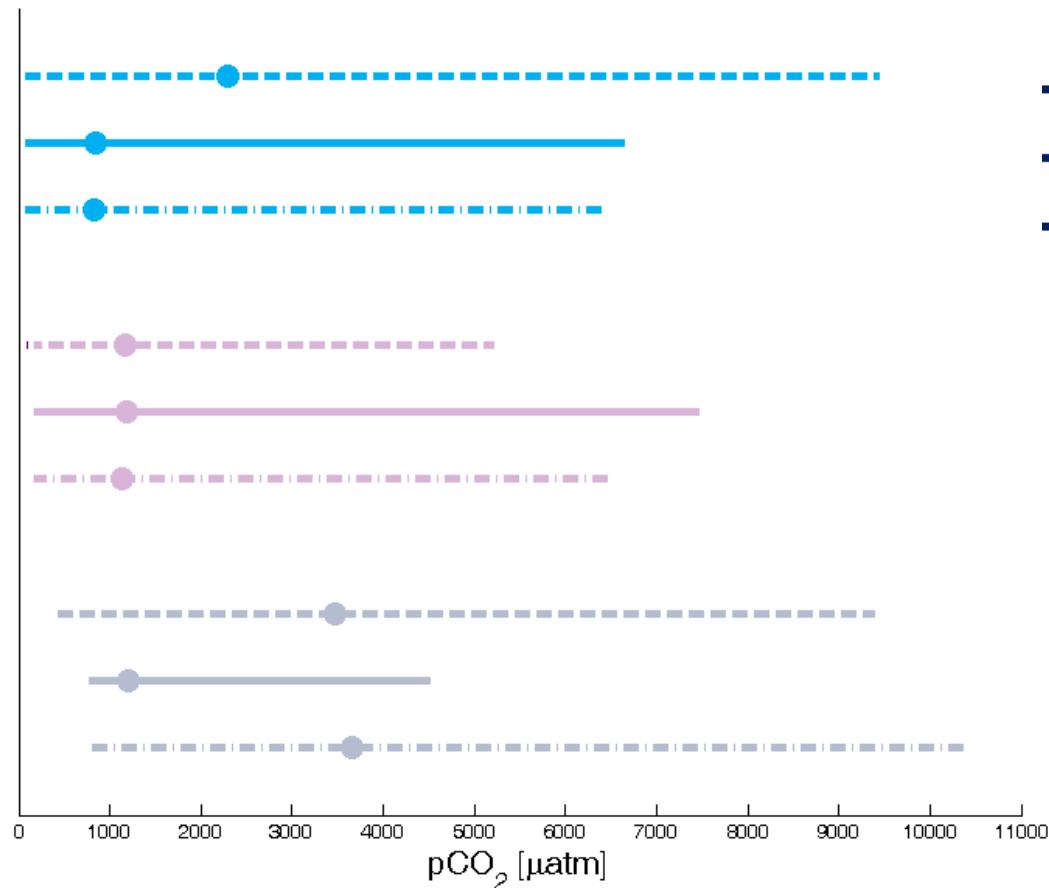
ALK ~ 3470  $\mu\text{eq L}^{-1}$   
DOC ~ 9.4  $\text{mg L}^{-1}$

## Med ALK

ALK ~ 544  $\mu\text{eq L}^{-1}$   
DOC ~ 4.5  $\text{mg L}^{-1}$

## Low ALK

ALK ~ 12.5  $\mu\text{eq L}^{-1}$   
DOC ~ 14.2  $\text{mg L}^{-1}$



-- pCO<sub>2</sub>-DIC-ALK  
— pCO<sub>2</sub>-pH-ALK  
-·- pCO<sub>2</sub>-pH-DIC

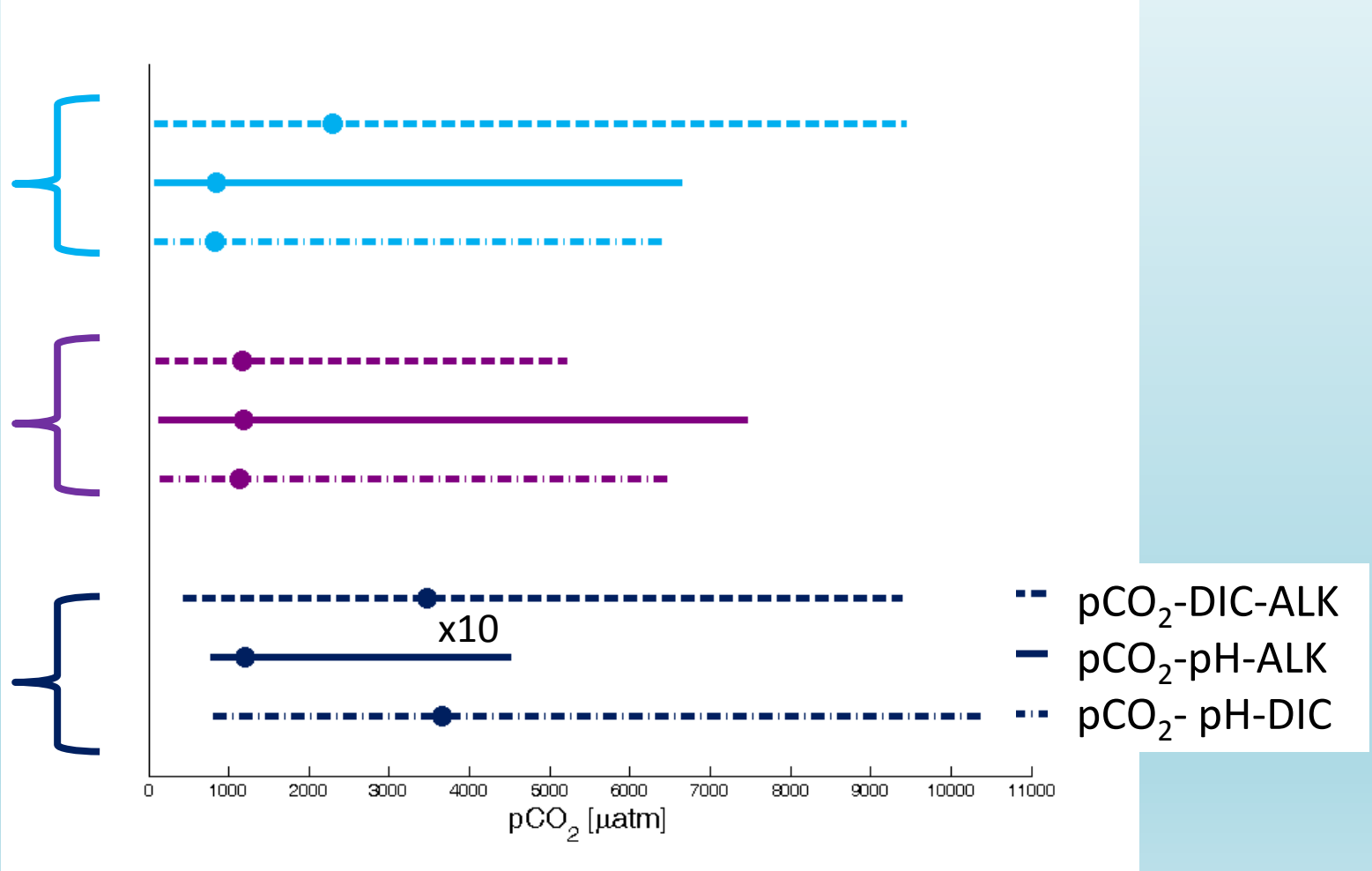
# Wide breath and skewed distribution of estimated pCO<sub>2</sub>

- Possible difficulty in constraining CO<sub>2</sub> concentrations

**High ALK**  
ALK ~ **3470** μeq L<sup>-1</sup>  
DOC ~ **9.4** mg L<sup>-1</sup>

**Med ALK**  
ALK ~ **544** μeq L<sup>-1</sup>  
DOC ~ **4.5** mg L<sup>-1</sup>

**Low ALK**  
ALK ~ **12.5** μeq L<sup>-1</sup>  
DOC ~ **14.2** mg L<sup>-1</sup>



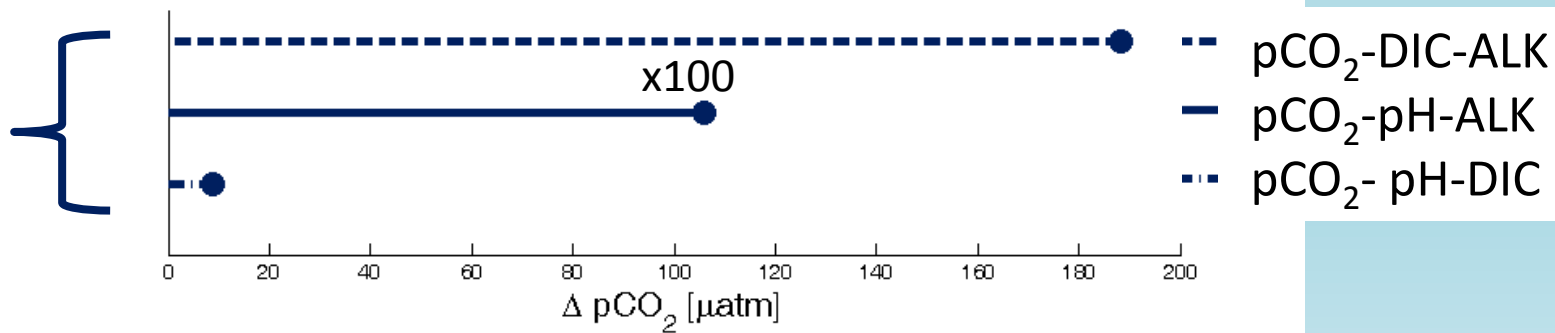


# pCO<sub>2</sub> bias due to random error

0.2% - 88%

## Low ALK

ALK ~ **12.5**  $\mu\text{eq L}^{-1}$   
DOC ~ **14.2**  $\text{mg L}^{-1}$



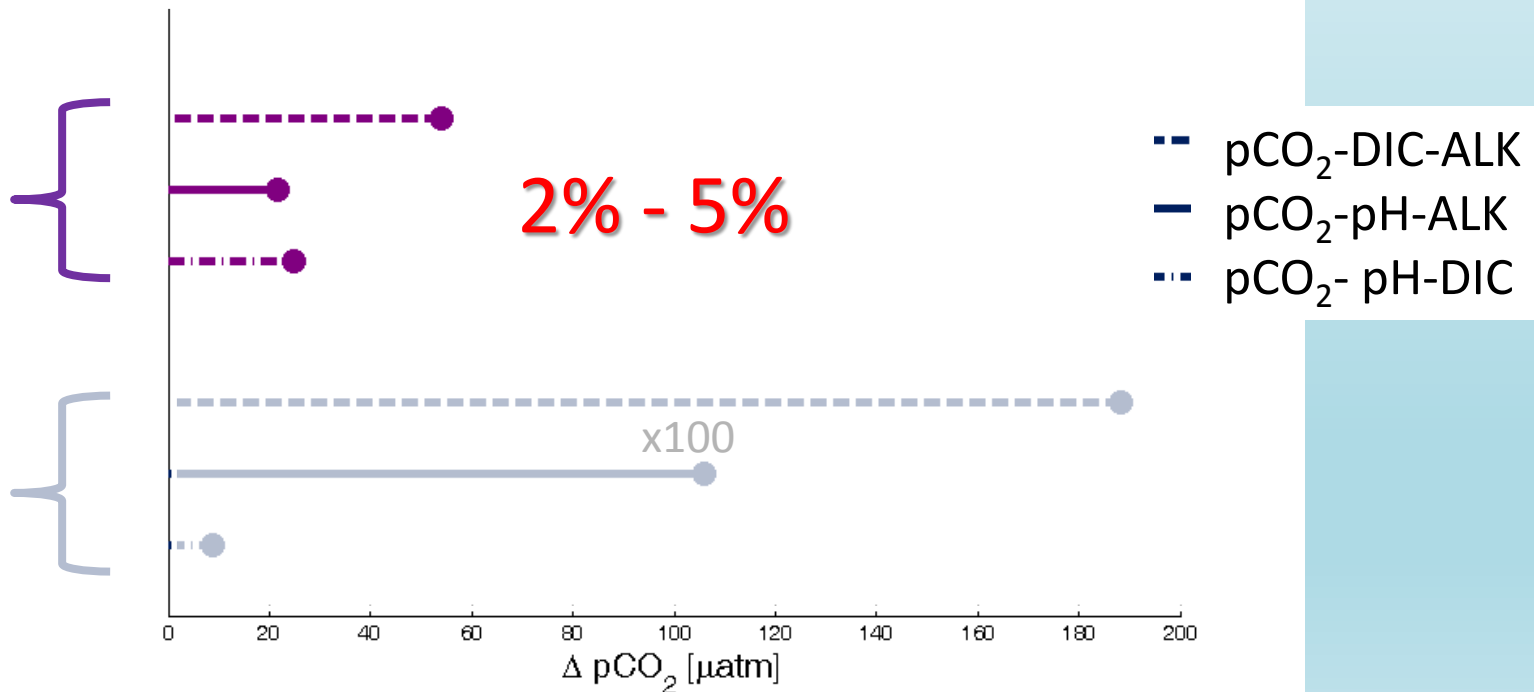
# pCO<sub>2</sub> bias due to random error

## Med ALK

ALK ~ 544  $\mu\text{eq L}^{-1}$   
DOC ~ 4.5  $\text{mg L}^{-1}$

## Low ALK

ALK ~ 12.5  $\mu\text{eq L}^{-1}$   
DOC ~ 14.2  $\text{mg L}^{-1}$



# pCO<sub>2</sub> bias due to random error

## High ALK

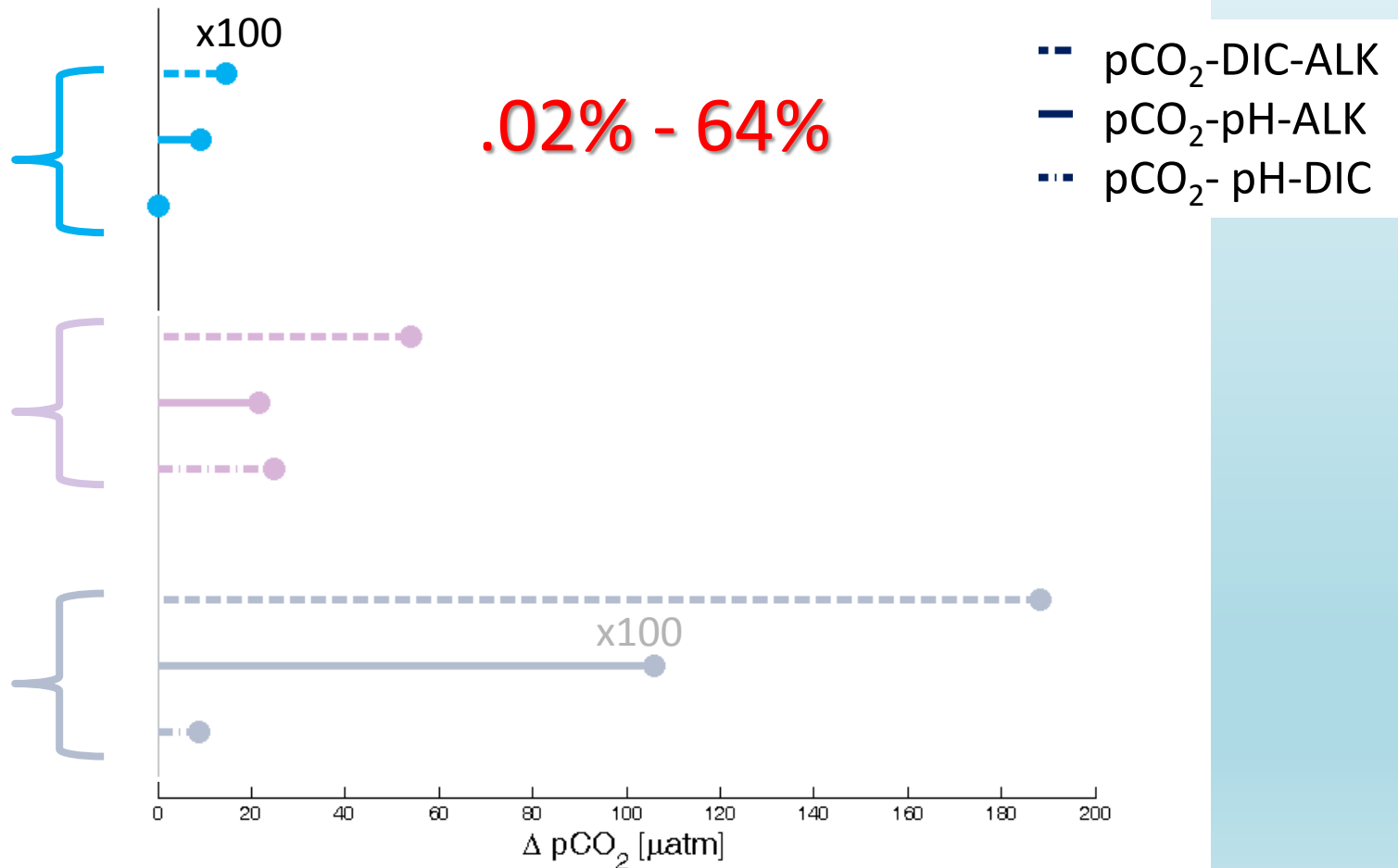
ALK ~ **3470**  $\mu\text{eq L}^{-1}$   
DOC ~ **9.4**  $\text{mg L}^{-1}$

## Med ALK

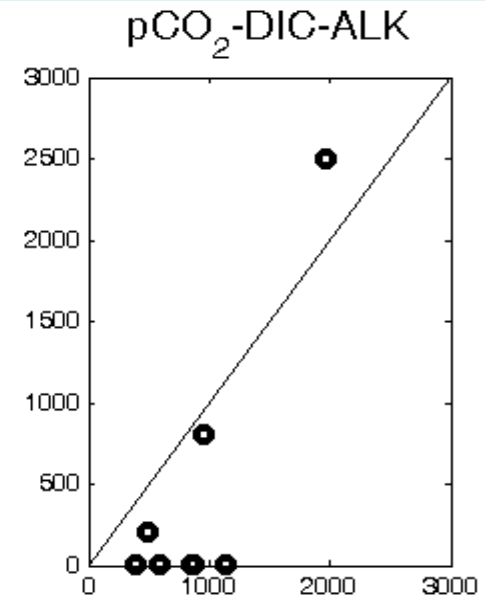
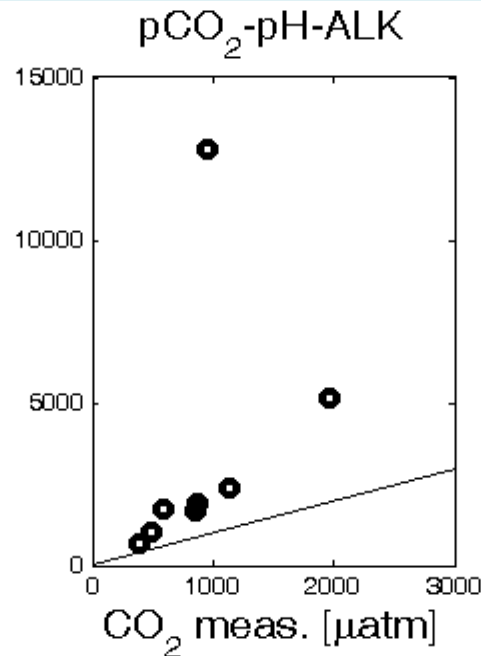
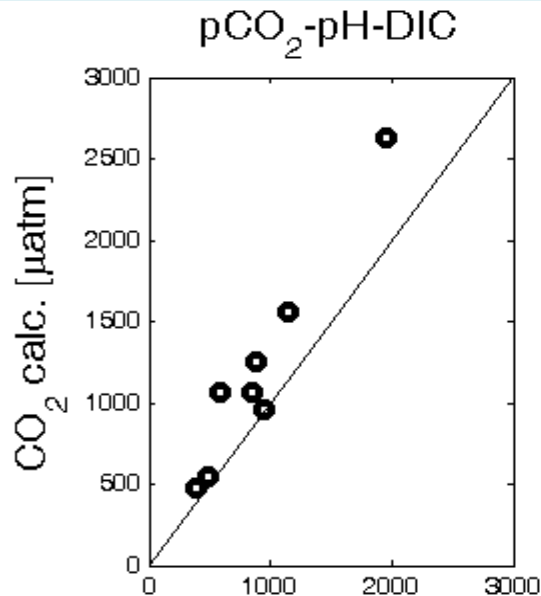
ALK ~ **544**  $\mu\text{eq L}^{-1}$   
DOC ~ **4.5**  $\text{mg L}^{-1}$

## Low ALK

ALK ~ **12.5**  $\mu\text{eq L}^{-1}$   
DOC ~ **14.2**  $\text{mg L}^{-1}$



# Random error is not the largest source of uncertainty



RMSE = **364** µatm

Low ANC = 9.0

Med ANC = 25.0

High ANC = 0.17

RMSE = **4410** µatm

Low ANC = 10,590

Med ANC = 22.0

High ANC = 9.0

RMSE = **675** µatm

Low ANC = 188.0

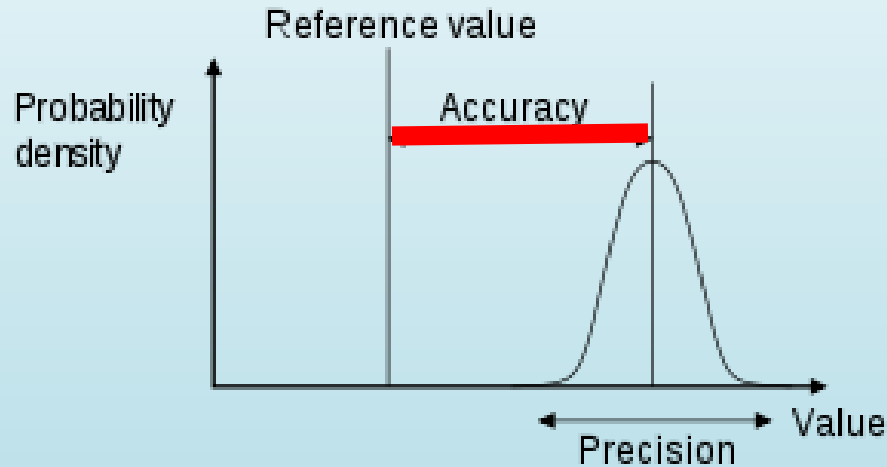
Med ANC = 54.0

High ANC = 1,456

# Take home messages

- There is no one perfect carbonate equilibrium model applicable for all lake groups, but model  $p\text{CO}_2$ -pH-DIC seems to be least affected by random error
- Carbonate equilibrium models cannot be blindly used to estimate  $\text{CO}_2$  concentrations and C flux from inland waters
- Random parameter errors are not the largest sources of uncertainty in the  $p\text{CO}_2$  calculation but need to be considered during data analysis and interpretation
  - Conservative estimates of uncertainty in  $\text{CO}_2$
  - Need to quantify other sources of uncertainty

# Next steps: Quantify systematic errors



**Systematic error** affects **accuracy**

- Instrumental errors
- Methodological limitations
- Personal errors

**Random error** affects **precision**

- Caused by many hard to control variables

# Acknowledgements

- Funding:
  - NSF DEB-0845166
  - NTL-LTER
  - CCR
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